

QUS 4022 IS 3049

(6.1)

$$\vec{\Sigma F} = \sum_i m_i \vec{a}_i = M \vec{a}_{cm}$$

$$\vec{a}_{cm} = \frac{d^2 \vec{r}_{cm}}{dt^2}$$

$$\vec{r}_{cm} = \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2 + m_3 \vec{r}_3}{m_1 + m_2 + m_3}$$

$$= \frac{10^{-3} [0.05 (2t \hat{i} - 5t^2 \hat{j}) + 0.02 (5 \hat{i} + 2t \hat{j}) + 0.01 (4t \hat{i} - 3 \hat{j})]}{[0.05 + 0.02 + 0.01] \times 10^{-3}}$$

$$= \frac{(0.1t + 0.1 + 0.04t) \hat{i} + (-0.25t^2 + 0.04t - 0.03) \hat{j}}{0.08}$$

$$= \frac{(0.14t + 0.1) \hat{i} + (-0.25t^2 + 0.04t - 0.03) \hat{j}}{0.08}$$

$$\vec{a}_{cm} = \frac{d^2 \vec{r}_{cm}}{dt^2} = \frac{1}{0.08} (-2)(0.25) \hat{j} \quad \text{[Crossed out terms: } \frac{-2+25}{8} \hat{j}]$$

$$\therefore \vec{\Sigma F} = M \vec{a}_{cm} = (0.08) \times 10^{-3} \frac{(-2)(0.25)}{0.08} \hat{j}$$

$$= -0.5 \hat{j} \times 10^{-3} \text{ N}$$

$$= -5 \times 10^{-4} \hat{j} \text{ N} \quad \#$$

(6.2)

$$\vec{p} = M \vec{v}_{cm}$$

$$\vec{v}_{cm} = \frac{d\vec{r}_{cm}}{dt} = \frac{(0.14)\hat{i} + (-0.5t + 0.04)\hat{j}}{0.08}$$

$$\vec{p} = \frac{[0.08 \times 10^{-3}] [(0.14)\hat{i} + (-0.5t + 0.04)\hat{j}]}{0.08}$$

$$= [14\hat{i} + (-50t + 4)\hat{j}] \times 10^{-5} \text{ kg m/s}$$

$$\vec{p}(t=2\text{ s}) = 14\hat{i} - 46\hat{j} \quad \text{kg m/s}$$

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(6.3) use (6.1)